CONTRIBUTION FROM THE W. **A.** NOYES CHEMISTRY LABORATORY AND THE MATERIALS RESEARCH LABORATORY, UNIVERSITY OF ILLINOIS, URBANA, ILLINOIS 61801

The Crystal Structure of Sodium 12-Niobomanganate(IV), $Na_{12}MnNb_{12}O_{38}\cdot 50H_2O_1$

BY C. M. FLYNN, JR., AND G. D. STUCKY

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Sodium 12-niobomanganate(IV), Na₁₂MnNb₁₂O₈₃.50H₂O, is monoclinic, $a = 24.18 \pm 0.03$ Å, $b = 12.69 \pm 0.02$ Å, $c = 14.14$ \pm 0.02 Å, β = 92.1 \pm 0.2°, Z = 2, ρ_{exptl} = 2.31 g/cm³, ρ_{calo} = 2.26 g/cm³, space group P₂₁/n, all at 24-25°. Data were collected photographically. The structure was refined by Fourier, difference Fourier, and full-matrix least-squares methods to an *R* value of 11.7% for 3263 observed reflections. The structure is composed of sodium ions, water molecules, and anions $MnNb₁₂O₃₈¹²$. The anion consists of a manganese atom octahedrally coordinated by oxygen atoms from two Nb₈O₁₉ groups, the latter having first been found by Lindqvist in $Na_7HNb_8O_{10} \cdot 15H_2O$. The anion has a crystallographic center of symmetry, but approximates D_{sd} symmetry. The Mn-O distances are equal within experimental error $(\sigma = 0.03 \text{ Å})$, averaging 1.87 Å, but the MnO₆ octahedron is stretched along the pseudo-threefold axis of the anion. The Nb-O distances range from 1.75 to 2.43 Å ($\sigma = 0.03$ Å), depending on the chemical environment of the oxygen atom. The packing of the anions correlates with the optical properties of the compound. The unit cell of trigonal Na_2Li_1 ₀ $\text{MnNb}_2\text{O}_{38}$.44H₂O was also determined.

Introduction

Since Keggin first described the structure of the PW_{12} - O_{40} ³⁻ ion,² the structures of several isopoly and heteropoly complexes have been reported. A review of these structures published in 1956³ has been augmented by a recent general review of isopoly complexes.⁴ Wells also reviews them in his book.⁵ However, in most of these studies, only heavy-atom positions were determined, and anion oxygen atom positions were inferred qualitatively from packing considerations. Recent advances in data collection and computation have made complete determinations feasible-examples include two salts of the $V_{10}O_{28}$ ⁶⁻ anion^{6,7} and $Na_3[H_6CrMo_6O_{24}].$ $8H₂O⁸$

In some studies of transition metal heteropolyniobates,^{1,9} we have obtained several salts of a manganese-(IV) complex. To establish the structure of the anion, we have carried out a single-crystal X-ray structure determination of the sodium salt, $\text{Na}_{12}\text{MnNb}_{12}\text{O}_{38} \cdot 50\text{H}_{2}\text{O}$, which we report here. In the course of this work, we also determined the unit cell of $Na₂Li₁₀MnNb₁₂O₃₈$. 44H20.

Experimental Section

 $Compounds.$ The 12-niobomanganate (IV) complex is prepared by the reaction of manganese(I1)-EDTA complex and a stoichiometric quantity of sodium 6-niobate with hydrogen peroxide in a hot aqueous solution. Details are given elsewhere.⁹

Unit Cell and Space Group of $\text{Na}_2\text{Li}_{10}\text{MnNb}_{12}\text{O}_{38}\cdot44\text{H}_2\text{O}$. Fragments of the thin plates of this optically uniaxial compound were mounted with epoxy cement in 0.5-mm diameter thin-walled glass capillaries filled with $1:2 \frac{\nu}{\nu}$ ethanol-water to prevent loss of water of crystallization and sealed with epoxy cement. Since decomposition of the crystals occurred at room temperature, the rotation and zero-level Weissenberg photographs were taken at 0-4°, using Cu K α radiation (λ 1.5418 Å, Ni filter). The *c* axis was perpendicular to the rotation axis, and the $\overline{1210}$ direction was parallel to it. The photographs showed that the crystal was not single, but unit cell data could still be obtained. Attempts to obtain a single crystal were unsuccessful.

The unit cell constants obtained were $a = 12.03 \pm 0.03$ Å and $c = 3 \times (14.76 \pm 0.03)$ $\AA = 44.3 \pm 0.1$ \AA . The density at 27^c (flotation in 1,2-C₂H₄Br₂-CH₂I₂) was 2.40 \pm 0.02 g/cm³; that calculated for three formula weights per unit cell is 2.41 g/cm3.

Under the microscope, etch pits were observed on the (0001) faces of the crystals as they dissolved while the ethanol evaporated from the ethanol-water immersion medium. 'These had trigonal symmetry. Pits on one side of a plate were oriented oppositely from those on the other side. Where two of these merged, a hexagonal hole formed, These observations require that the crystal be trigonal, without a mirror perpendicular to c . The possible point groups are thus $3, 3, 32, 3m$, and $3m$. From zero-level Weissenberg photographs $(I(h0\bar{h}l) = I(h0\bar{h}l))$, oscillation photographs, and the etch pit data, the Laue group was determined to be $\overline{3}m$. The possible point groups are now 32 and $\overline{5}m$. 3m. For reflections *0001,* systematic absences were observed to occur for $l \neq 3n$. The possible space groups are therefore the enantiomorphous set $P3₂12$ and $P3₁12$.

 $\textbf{Unit Cell}$ and $\textbf{Space Group}$ of $\textbf{Na}_{12}\textbf{MnNb}_{12}\textbf{O}_{38}$. $\textbf{50}\textbf{H}_{2}\textbf{O}$.---The rod crystals of the compound cleave easily perpendicular to the long direction. Cleaved fragments were mounted in $1:3$ v/v ethanolwater as immersion medium to prevent loss of water of crystallization. Rotation and Weissenberg photographs were taken at 25° using Cu K α radiation (Ni filter). The length of the rod was aligned parallel to the rotation axis. Precessiop photographs were also taken, using Mo K α radiation (λ 0.7107 Å, Zr filter), at 25'. The rod length was aligned parallel to the dial axis. The precession camera was calibrated with a single crystal of NaC1, $a = 5.6280 \text{ Å}.$

Sodium 12-niobomanganate(IV)-5O-water is monoclinic with the rod length parallel to *b.* Unit cell constants from *hkO* and *Oki* precession photographs are $a = 24.18 \pm 0.03 \text{ Å}$, $b = 12.69 \pm 0.02$ A, $c = 14.14 \pm 0.02$ A, and $\beta = 92.1 \pm 0.2^{\circ}$. The density measured at 24° (flotation in 1,2-C₂H₄Br₂-CH₂I₂) was 2.31 \pm 0.02 g/cm3; because of efflorescence, measurements were made rapidly using large (up to 2-mm) crystals. The density calculated for two formula weights per unit cell is 2.26 g/cm3. The high observed density relative to the calculated density is attributed to loss of water from the crystals during the density determination.

⁽¹⁾ Taken from the Ph.D. dissertation of C. M. Flynn, Jr., University of Illinois, 1967.

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⁽⁷⁾ A. G. Swallow, P. R. Ahmed, and W. H. Barnes, *Acta Cvyst.,* **21,** 397 (1966).

⁽⁸⁾ **A.** Perloff, Ph.D. Dissertation, Georgetown University, 1967; presented at the American Crystallographic Association Meeting, Georgia Institute of Technology, Atlanta, Ga., Jan 25-28, 1967.

⁽⁹⁾ C. M. Flynn, Jr., and G. D. Stucky, *Inovg. Chem.,* **8,** 332 (1969).

Comparison of the Weissenberg *h02* and hl2 photographs shows that the unit cell is primitive. For reflections *h01* there were systematic absences for $h + l = 2n + 1$. The zero-level precession photographs revealed systematic absences for reflections *OkO* of the type $k = 2n + 1$. The space group is therefore uniquely P_{21}/n .

Collection and Reduction of Data for the Sodium Salt.--- Data were collected at room temperature using Mo *Ka* radiation (A 0.7107 **A,** Zr filter, *32.5* **kV,** 20 m.4) and multiple-film equiinclination Weissenberg technique (Supper camera). Crystals were mounted in the same way as for the unit cell measurements. Two crystals were used, each of roughly cylindrical dimensions, about 0.30 mm long and about 0.10 mm in diameter. For the first crystal, two exposures (IS and 72 hr) of six-film packs were made for each of the levels $h0l$ through $h6l$. For the second crystal (used owing to a mishap), one exposure (96 hr) of a sixfilm pack was taken for each of the levels *h61* through h141.

The spot (13, 0, 3) was photographed for measured numbers of oscillations (time series $(1.3)^n$) to furnish calibrated intensity strips for visual estimation of intensities. Only spots on the top halves of the films were measured, these all being symmetry independent.

For a given level, all films were scaled to the most intense one in the series. The data were first all scaled together by exposure times and data common to the two crystals. The observed intensities (numbering over 3300) were corrected for Lorentz, polarization, and spot-extension effects. The absorption coefficient μ/ρ was calculated using data from the "International Tables for X-Ray Crystallography."¹⁰ The value obtained was $\mu/\rho = 8.0 \text{ cm}^2/\text{g}$. From the calculated density of 2.26 g/cm³, the value of μ is 18 cm⁻¹. For a cylinder of radius 0.05 mm, μR $= 0.09$. An absorption correction was therefore considered unnecessary. To the accuracy that the crystal can be described as a cylinder, the maximum error in the data made by neglecting absorption is 2% .

About 100 reflections were discarded to beam-stop interference or bad streaking. These were mostly of the types *lkO, 2k0, Okl,* 1kl, $\bar{1}$ kl, 2kl, and $\bar{2}$ kl. There remained 3264 independent observed reflections.

Structure Solution

Calculations were performed on the IBM 7094 computer of the University of Illinois Department of Computer Science. A three-dimensional Patterson map was calculated using the fast ERFR3 program of Sly, Shoemaker, and van den Hende.¹¹ The most prominent feature was a group of 18 strong peaks symmetrically arranged about the origin. Another set of strong peaks appeared about the point $(1/2, 1/2, 1/2)$. Because of the complexity of the Patterson function, indications of the structure of the 12-niobomanganate(IV) anion were obtained by indirect means

The structure of the 12-niobomanganate(IV) ion was suggested by considering the structural features of known isopoly and heteropoly complexes and the physicochemical properties of the 12-niobomanganate(IV) compounds. The former considerations suggested a compact, symmetrical structure in which the niobium atoms were octahedrally coordinated by oxygen atoms. Further, these octahedra would be packed together sharing edges and corners but not faces. The properties of the 12-niobomanganate (IV) compounds are consistent with 38 oxygen atoms per complex anion and support octahedral coordination of the manganese atom. Two models were found which satisfied all of these conditions. In one model, which has ideal symmetry O_h , the niobium atoms are arranged in a cuboctahedron about the manganese atom. The other, having ideal symmetry D_{3d} , consists of two Nb_6O_{19} groups¹² coordinated to the manganese atom.

The positions of the manganese atoms in the unit cell, which are completely fixed by symmetry, were taken as $(0, 0, 0; \frac{1}{2}, \frac{1}{2}, \frac{1}{2})$. From the Patterson map, the distance between niobium atoms across edge-shared octahedra was about 3.3 Å; this distance agrees with Lindqvist's results for sodium 6-niobate¹² (Nb-Nb = 3.3-3.4 Å). All the heavy metal-heavy metal vectors of the Patterson map were found to give excellent agreement with the proposed D_{3d} model, with the pseudothreefold axis of the anion lying approximately in the *ab* plane at an angle of about 20" to *a.*

This model is consistent with the following observations. (1) The length of the D_{sd} ion is about 14 Å, using a closest metal-metal distance of 3.3 Å^{12} across edgeshared octahedra, metal-oxygen distances of 2.0 Å , and a van der Waals radius of 1.4 Å for oxygen. Since this is longer than the *b* cell edge (12.69 *K),* the anion cannot be aligned in this direction. (2) The ease of formation of the complex from alkali $Nb_6O_{19}^{8-}$ salts, manganese(II), and oxidizing agent⁹ is consistent with the presence of Nb_6O_{19} groups in the heteropolyanion. (3) The infrared spectrum of the potassium sodium 12-niobomanganate is very similar to that of sodium or potassium 6-niobate in the $500-1000$ -cm⁻¹ region where the metal-oxygen vibrations occur.⁹ (4) The optical anisotropy of crystals of this complex implies deviation from cubic symmetry in the crystal field about the manganese atom. *(5)* Since the trigonal lithium-sodium salt contains three formula weights per unit cell, there is no proof of threefold symmetry in the anion. The space group requires only twofold symmetry. However, the unit cell dimensions still constrain the anions to lie with their threefold axes more nearly parallel to c than to *a.* Under polarized light these crystals are bright orange with the polarization plane perpendicular to c and light orange-yellow in parallel orientation. Crystals of the sodium salt are bright orange when the *a* axis is most nearly perpendicular to the polarization plane and yellow in the other two principal orientations. Combination of all of these data suggests that in the sodium salt the anions lie with their threefold axes close to the *a* axis.

Refinement

Fourier calculations were done with the ERFR3 program." Structure factors were initially calculated using a routine taken from the UCLh least-squares program of Gantzel, Sparks, and Trueblood.¹⁸ Scale factors were obtained initially for each layer by the rela-

^{(10) &}quot;International Tables for X-Ray Ciystallogiaphy," Vol. **3,** The Kynoch Press, Birmingham, England, 1962, **p** 162.

⁽¹¹⁾ W. G. Sly, D. P. Shoemaker, and J. H. van den Hende, **"A** Two and Three Dimensional Fourier Program for the IBM 709/7090, ERFR-2," **Esso** Research Report CBRL22M-62, Linden, N. J., 1962.

⁽¹²⁾ I. Lindqvist, *Arkiv &mi,* **5, 247** (1953).

⁽¹³⁾ P. K. Gantzel, R. **A.** Sparks, and K. N. Trueblood, UCLAS1, 1961

tion $K_{\text{layer}} = \Sigma(F_o)_{\text{layer}} / \Sigma(F_o)_{\text{layer}}$. Later this program was rewritten by the authors to take better advantage of symmetry elements, thereby saving computer time. Least-squares calculations were done with ORFLSD, a modification of the full-matrix least-squares program ORFLS of Busing, Martin, and Levy.14 During refinement, interatomic distances were calculated with DISTAN, a bond distance and angle program by Shoemaker,16 with local modifications.

Owing to storage limitations, a complete refinement cycle consisted of refinement of the more than 220 variable parameters in two or three batches. One complete refinement cycle required about 1 hr of IBM 7094 computer time. The function minimized was $\sum w(|F_0| |F_{\rm e}|^2$ with w always set equal to 1 for all observed reflections. Unobserved reflections were not included in the refinement.

Scattering factors for neutral Nb, Mn, and O atoms and for Na+ and **F-** were taken from the "International Tables".¹⁶ Real and imaginary corrections for anomalous scattering (Mo *Ka* radiation) were applied to Mn and Nb. Trial initial isotropic temperature factors *B* were $(in \mathbf{A}^2)$: 3.0 for Mn, 4.0 for Nb, and 4.5 for light atoms.

Trial niobium positions obtained from well-resolved Patterson peaks were refined using only the 378 strongest reflections, after having discarded one reflection (002) which appeared to be badly affected by extinction. The value of R^{17} fell to 24% during this refinement. With 575 high-angle reflections temporarily omitted, Fourier calculations using the 2688 remaining reflections then revealed 19 anionic oxygen atoms in their expected positions, as well as 31 other prominent peaks. These 31 atoms, called X atoms below, were assigned fluoride ion scattering factors at this point, since distinction between sodium ions and water molecules could not be made reliably on the basis of peak heights. The value of *R* over the 2688 reflections was 34% including only the heavy atoms and dropped to 29% on including the light atoms. Next, the X atom positions and the heavy-atom isotropic temperature factors were refined, giving $R = 21\%$.

The high-angle reflections were then returned to the calculations, and niobium and light-atom positional parameters and the isotropic temperature factors were refined once. The *R* value was then 13% . The stereochemistry of three of the X atoms, combined with their low temperature factors, then indicated that they might be sodium ions. Two of these X atoms had coordination octahedra with a face in common. While this stereochemistry is not unknown for sodium salts,18 it was intuitively dissatisfying here, because it was thought that a more uniform distribution of sodium ions would most effectively counter the high anion charges. However, additional Fourier calculations (including

(16) Reference 10, pp 202, 203, 210, 211, 215, 216.

(17) $R = \sum_{i} (||F_{o}|-|F_{c}||)/\sum(|F_{o}|)$.

one in which only anion atoms were input) only confirmed the arrangement of X atoms. The identities of three more expected sodium ions were still not evident. Another refinement cycle was carried out, with these three X atoms put in as sodium ions and the other 28 put in as oxygen atoms. The value of *R* was 12% and the value of wR^{19} was 14.3%. A difference map was then calculated, in which several X atoms were omitted because their temperature factors were excessively high, casting doubt on their positions. The result indicated that two of these X atoms were probably spurious or were subject to disorder. Because these two atoms also had the highest temperature fac-

TABLE I POSITIONAL PARAMETERS AND ISOTROPIC TEMPERATURE FACTORS OF ATOMS[®]

Atom	x	У	z	В
	0			
Mn	0.2187(1)	0 $-0.0249(3)$	0	0.57(12)
Nb(1)	0.1076(1)		$-0.0132(2)$	0.83(6)
Nb(2)		$-0.0259(3)$	0.1170(2)	0.70(6)
Nb(3)	0.0962 (1) 0.0626(1)	$-0.0173(3)$	$-0.1312(2)$	0.68(5)
Nb(4)	0.1870(1)	0.2086(3)	0.0003(2)	0.60(6)
Nb(5)	0.1769(1)	0.1885(3) 0.1956(3)	0.1111(2)	0.73(6)
Nb(6) O(1)	0.0420 (10)	0.0817(19)	$-0.1241(2)$	0.85(6)
O(2)	0.0336(10)	0.0846(20)	0.0870(17)	0.7(4)
O(3)	0.1397(19)	0.0863(18)	$-0.0890(18)$ $-0.0048(16)$	1.2(6) 0.2(3)
O(4)	0.1458(10)	0.0861(20)	0.1882(17)	1.0(4)
O(5)	0.1290(11)	0.0935(21)	$-0.2047(18)$	1.4(5)
O(6)	0.2415(10)	0.0755(19)	0.0889(16)	0.9(4)
O(7)	0.2308(10)	0.0819(19)	$-0.1104(16)$	0.8(4)
O(8)	0.0063(12)	0.2972(25)	0.0055(21)	2.1(6)
O(9)	0.1114(10)	0.2554(21)	0.1017(18)	1.1(5)
O(10)	0.1030 (9)	0.2618(19)	$-0.1011(16)$	0.6(4)
O(11)	0.2058(11)	0.2598(22)	$-0.0053(19)$	1.5(5)
O(12)	0.2232(14)	0.2652(29)	0.1953(25)	3.8(7)
O(13)	0.2088 (12)	0.2827(25)	$-0.2077(21)$	2.5(6)
O(14)	0.0651(10)	$-0.0780(20)$	$-0.0065(17)$	0.7(4)
O(15)	0.0839(12)	$-0.1084(24)$	0.2095(20)	2.3(6)
O(16)	0.0655 (12)	$-0.0941(24)$	$-0.2245(20)$	2, 1(6)
O(17)	0.1734(10)	$-0.0931(19)$	0.0818(17)	0.8(4)
O(18)	0.1642(11)	$-0.0901(21)$	$-0.1044(18)$	1.3(5)
O(19)	0.2782(11)	$-0.1063(23)$	$-0.0160(20)$	1.9(5)
Na(1)	0.1278(7)	$-0.0437(14)$	0.4906(12)	2.3(3)
$\rm Na(2)$	0.2572(7)	0.0646(16)	0.4273(14)	2.7(4)
Na(3)	0.3620 (7)	0.0674(15)	0.2963(13)	2.6(4)
Na(4)	0.3494 (15)	0.1064(32)	$-0.3179(27)$	14.7(9)
Na(5)	0.0483(18)	0.3401(32)	0.3610 (78)	13.8(7)
W(1)	0.0360 (18)	$-0.0057(38)$	0.4287(32)	5.9(10)
W(2)	0.2733(11)	0.4282(23)	$-0.0330(20)$	1.8(5)
W(3)	0.2710 (13)	$-0.0207(27)$	0.2711(22)	2.5(6)
W(4)	0.2716(13)	$-0.0027(28)$	$-0.2844(24)$	3.4(7)
W(5)	0.4340 (27)	0.0066(58)	0.0396(47)	10.7(19)
W(6)	0.3515(14)	0.0005(30)	0.4556(25)	3.6(7)
W(7)	0.1635(11)	0.0900(22)	0.3805(20)	1.7(5)
W(8)	0.1337(14)	0.0970(28)	$-0.3949(24)$	3.1(7)
W(9)	0.3515(14)	0.1165(29)	0.1333 (25)	3.1(7)
W(10)	0.3468(25)	0.1360(52)	$-0.1037(42)$	11.1(5)
W(11)	0.0432(14)	0.1623(28)	0.2851 (24)	3.4(7)
W(12)	0.0189 (19)	0.1595(40)	$-0.2930(34)$	6.2(11)
W(13)	0.2420(13)	0.1783(28)	$-0.4411(23)$	2.8(7)
W(14)	0.3887 (20)	0.1986 (43)	$-0.4545(34)$	6.4(11)
W(15)	0.4401(14)	0.1852(29)	0.3302(24)	3.2(6)
W(16)	0.4581(26)	0.1736(60)	$-0.2723(47)$	12.6 (16)
W(17)	0.2960 (10)	0.2060(21)	0.3426(18)	1.3(4)
W(18)	0.3118(15)	0.2596(30)	$-0.2624(26)$	3.6(7)
W(19)	0.3496(13)	0.3412(26)	0.1406(23)	2.6(6)
W(20)	0.4041 (16)	0.3380(31)	$-0.1015(27)$	4.0(8)
W(21)	0.0833(16)	0.4183(34)	0.2170(28)	4.4(8)
W(22) W(23)	0.4101(23)	$-0.0383(51)$	$-0.3366(41)$	9.2(13)
W(24)	0.1528(18)	0.3146(37)	0.3729(31)	5.2(10)
	0.1372(19)	0.3590(38)	$-0.3654(34)$	5.9 (10)

*^a*In this and succeeding tables, the number in parentheses after each quantity **is** its standard deviation in units of the last significant figure.

(19) $wR = \left[\Sigma w(|F_0| - |F_0|)^2 / \Sigma w(F_0)^2\right]^{1/2}; w = 1.$

⁽¹⁴⁾ W. R. Busing, K. 0. Martin, and H. A. Levy, Report ORNL-TM- 305, Oak Ridge National Laboratory, Oak Ridge, Tenn., 1962.

⁽¹⁵⁾ D. P. Shoemaker, Massachusetts Institute of Technology, 1963.

⁽¹⁷⁾ $R = \sum_{i} (|F_o| - |F_e|)/\sum(|F_o|)$.
(18) P. B. Jamieson and L. S. D. Glasser, *Acta Cryst.*, **22**, 507 (1967).

TABLE I1

OBSERVED AND CALCULATED STRUCTURE FACTORS IN ELECTRONS FOR Na12MnNb12O₁₈ · 50H₂O

TABLE II (Continued)

tors, they were eliminated from the structure. This decision was reinforced by the fact that some excessively short (less than 2.3 **A)** interatomic distances were eliminated simultaneously. In addition, the distances between peaks suggested that two more X atoms were sodium ions, despite their low peak heights, which were then attributed to partial site occupation. The stereochemistry failed to indicate the identity of an expected sixth sodium ion; this is attributed to disorder and will be discussed below.

The last two refinement cycles were run with five **X** atoms input as sodium ions. In the first cycle, the layer scale factors and all niobium and anion oxygen atom positions were varied in the first round of calculations, then the layer scale factors and all sodium and water-oxygen positions in the second round, and finally all of the isotropic temperature factors in the third round. In the second cycle, the first 115 parameters were varied and then the final 117 parameters. The largest value in the correlation matrices for any of these runs was 0.20. The final value of *R* was 11.6 $\%$ and of wR , 14.0% for the 3263 observed reflections. In the last refinement, none of the 162 varied positional parameters shifted by more than 0.01 of its standard deviation. The final shifts of the scale factors were all less than half their standard deviations, which ranged from 0.7 to 2.2% . Of the 55 isotropic temperature factors, none shifted by more than 0.8 of its standard deviation. **A** final difference Fourier showed no peaks greater than 0.75 e/ \AA ³ or about 35% the average water-oxygen peak height. It should be reemphasized that because of the large number of heavy atoms, the instability of the crystals, and the existence of interstitial holes in the water matrix which readily permits a statistical disordering of sodium ions, a portion of the sodium-water matrix is not well defined. In particular, the errors

Figure 1.—Structure of the $MnNb_{12}Os_{81}^{12-}$ anion.

stated for $Na(4)$ and $Na(5)$ and their coordinated water molecules should be taken as a lower limit.

The large number of atoms relative to the amount of data did not justify refinement of anisotropic temperature factors. The financial expense of computations did not justify this either, as well as further attempts to improve the values of the parameters. Final positional parameters and isotropic temperature factors are given in Table I. Observed and final calculated structure factors, in electrons, are given in Table 11.

Discussion **of** the Structure

Final interatomic distances and bond angles, with their standard deviations, were calculated with the ORFFE program of Busing, Martin, and Levy.20 The DISTAN program16 was used to obtain distances connecting anionic and nonanionic atoms. Illustrations of the structure were prepared with the aid of the pro $gram$ ORTEP. 21

The bond lengths and angles in the $MnNb_{12}O_{38}^{12}$ anion, with their standard deviations, are given in Tables I11 and IV. Mean values for quantities equivalent by the pseudo-threefold symmetry are also given with the approximate maximum deviations of individual values from them.

The anion consists of a manganese(1V) atom coordinated to two Nb_6O_{19} groups¹³ as shown in Figure 1. The anion has symmetry D_{3d} within two standard deviations with respect to interatomic distances, but the deviations of some individual bond angles from their pseudo-symmetry mean values appear significant.

The mean Mn-O distance of 1.87 \pm 0.01 Å is about the same as the Mn–O distances in two forms of $MnO₂$ $(1.87-1.94 \text{ Å}^{22})$ and in $\text{Na}_{7}\text{H}_{4}\text{Mn}(\text{IO}_{6})_{3} \cdot 17\text{H}_{2}\text{O}$ (mean, 1.90 Å).²³ The mean O-Mn-O bond angle across the plane perpendicular to the pseudo-threefold axis is $96.7 \pm 0.3^{\circ}$; *i.e.*, the MnO₆ octahedron is stretched along a threefold axis. This stretching of the $MnO₆$ octahedron is attributed to electrostatic repulsion of the two Nb_6O_{19} groups. Consistent with this, the mean closest approach of oxygen atoms (not bonded to manganese) of the two niobate groups is 3.29 \pm 0.02 Å across the plane perpendicular to the pseudo-threefold axis. This is about 0.5 Å longer than the usual van der Waals contact distance.

Nine of the twelve niobium-niobium distances are in the range 3.3-3.4 Å, in agreement with Lindqvist's results for $Na₇HNb₆O₁₉·15H₂O₁₃$ Three niobium-niobium distances are longer, about 3.53 A, and these are bound to the face of the $Nb₆$ octahedron which faces the manganese atom. These three longer niobium-niobium distances are attributed to the additional electrostatic repulsion contributed by the manganese atom core.

The niobium-oxygen distances vary according to the number of bonds from the metal atoms to a given oxygen atom. The shortest Nb-O distances $(1.75-1.79 \text{ Å})$ correspond to terminal oxygen atoms, which each have only one bond to a niobium atom. Distances to oxygen atoms which bridge two niobium atoms range from 1.88 to 2.05 A. For oxygen atoms which bridge two niobium atoms and the manganese atom, the Nb-0 distances average 2.10 Å . The longest Nb-O distances connect the niobium atoms to the oxygen atom in the center of the Nb_6O_{19} group $(O(3))$ and average about 2.4 A. These long distances are a consequence of the niobium-niobium electrostatic repulsions. This variation of metal-oxygen distances has recently been found in two compounds containing the $V_{10}O_{28}^{6}$ anion,^{7,8} in $K_5Co^{III}W_{12}O_{40}.20H_2O^{24}$ and in $Na_3H_6Cr^{III}Mo_6O_{24}.$ $8H₂O.⁹$ In the 6-molybdochromate(III), the Mo-O distances range from 1.70 to 2.35 Å. The niobiumoxygen distances in a high-temperature form of $Nb₂O₅$ and in compounds of $Nb₂O₅$ with $TiO₂$ and $WO₃$ range from 1.7 to 2.2 Å.²⁵ In these ReO₃-based structures, however, no good correlation of Nb-0 distances with oxygen atom bonding was noted.

In the 12-niobomanganate(IV), the niobium atoms all have octahedral coordination of oxygen atoms. The shortest contacts to other oxygen atoms are about 3.7 Å $(Nb(2)-W(11)$ and $Nb(3)-W(12)$, too long for bonds. Niobium-oxygen coordination in oxides is nearly always octahedral; however, coordination number 7 has recently been found in the hydrothermally synthesized $NaNb₆O₁₅(OH).²⁶$ In a high-temperature form of Nb₂-*0;* there is some tetrahedrally coordinated niobium, but tetrahedral sites in some $Nb₂O₅-WO₃ compounds²⁵$ are probably occupied mainly by tungsten, in view of the stability of $WO₄²⁻$.

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 (4) (4) (4) (4) (4) (4) (4)

TABLE I11

^aQuantities equivalent **by** the pseudo-threefold symmetry of the anion are grouped together, and their average values are given with the approximate maximum range **of** individual values in units of the last significant figure.

 $O(17)-O(19)$ 2.94 (4) $O(18)-O(19)$ 2.99(4)

Mean 2.96 (5)

Within an Nb_6O_{19} group, the oxygen-oxygen distances corresponding to edges of $NbO₆$ oxtahedra are generally in the range 2.7-2.9 A. Qualitatively, the niobium atoms are electrostatically repelled away from the centers of slightly distorted oxygen octahedra, the bridging atoms being pulled inward. The temperature factors of the anionic oxygen atoms show some correlation with their chemical environment, being

greatest for terminal oxygen atoms (one Nb-0 bond) and least for the oxygen atom at the center of an Nb_6O_{19} group.

 $O(9)-O(10)$ 2.88 (4) $O(5)-O(18)$ 2.84 (4) $O(4)-O(17)$ 2.82(4) Mean 2.85 (3)

The packing of the anions in the unit cell is shown in Figure 2. The pseudo-threefold axes are canted $19.4 \pm$ 0.2° to the *a* axis, 70.6 \pm 0.2° to the *b* axis, and 1.7 \pm **0.2"** to the normal to the *ab* plane. The anion centered at $\left(\frac{1}{2}, \frac{1}{2}, \frac{1}{2}\right)$ is canted oppositely to that at $(0, 0, 0)$,

176.6 (11) 176.7 (11) 176.0 (12) 176.4 (4) 89.5(8) 89.3 (8) 89.1 (8) 89.3 **(2)** 93.6 *(8)* 95,2 (8) 93,l *(8)* 94.0 (11) 87.9 (8) *88,O* (8) 89.5 (8) 87.5 (8) 89.2 *(8)* 87.8 (8) 88.3 (10)

TABLE IV

a Quantities equivalent by the pseudo-threefold symmetry of the anion are grouped together, and their average values are given with the approximate maximum range of individual values in units of the last significant figure.

the two being related by the glide and twofold screw operations. The anions do not contact each other but are separated by water molecules. The shortest interanion distances are (in A): $4.20 (O(13) - O(19))$, 4.34 $(O(12)-O(17))$, 4.5₂ $(O(13)-O(18))$, and 4.8₁ $(C(13)-O(18))$ $O(19)$).

Interatomic distances and angles involving sodium ions and water molecules are given in Tables V and VI. The identification of sodium ions and water molecules is based on stereochemistry and temperature factors, as described under refinement of the structure.

Sodium-water distances vary from 2.3 to 2.8 Å. $\;$ The $\;$ coordination polyhedra of $Na(1)$, $Na(2)$, and $Na(3)$ are distorted octahedra. The octahedra about Na(1) and Na(2) have an edge in common, and the octahedra

about $Na(2)$ and $Na(3)$ have a face in common. (The distance Na(2)-Na(3) is 3.20 \pm 0.03 Å.) Face sharing by sodium-water octahedra has recently been found in $Na₂GeO₃·6H₂O$ and in the isomorphous silicate.¹⁸ Edge sharing by sodium-water octahedra is fairly common in highly hydrated sodium salts.²⁷⁻³⁰ The coordination of $Na(4)$ is irregular. Atom $Na(5)$ is surrounded by five water molecules at the corners of a distorted square pyramid. There are indications from difference maps that a sixth water molecule is sometimes

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TABLE VI11

TABLE VI

WATER-SODIUM-WATER ANGLES (DEG)

TABLE VI1

ANION-WATER CONTACTS $(\AA)^a$

Standard deviations are in the range 0.05-0.1 **A.**

Figure 2.-Packing of the anions in the unit cell, in *ac* projection, The heavy-metal atoms are near the centers of the octahedra, and the oxygen atoms are at the corners. The *b* cell direction runs down into the page.

present, completing a distorted octahedron about $Na(5)$.

Sodium-water distances in other compounds are comparable and vary widely, such that a standard sodiumwater distance is difficult to ascertain. Sodium-water distances in some other highly hydrated sodium salts are 2.41-2.49 Å in $Na_2S \cdot 9H_2O$ and $Na_2Se \cdot 9H_2O$,²⁸ 2.41-2.50 Å in $Na_2SiO_3.9H_2O^{27}$ 2.36-2.82 Å in Na₂- $SiO₃ \cdot 6H₂O$ and $Na₂GeO₃ \cdot 6H₂O₁¹⁸$ and 2.39-2.46 Å in $Na₂B₄O₇ \cdot 10H₂O₂$ ³⁰ In the compound $2Co(en)₃$ - $Cl_3 \cdot NaCl \cdot 6H_2O$, isolated sodium-water octahedra are present ; the sodium--oxygen distances are all equivalent, being $2.62 \text{ Å}.^{31}$

The results of chemical analyses¹⁰ require that six sodium ions exist in the asymmetric unit of the structure. That only five were found is attributed to disorder. In fact, difference maps show marked elongation of the $Na(4)$ peak, and the $Na(5)$ peak height is even lower than most oxygen peaks. The high calculated temperature factors of these two atoms are consistent with partial site occupation, since no allowance was made for the latter in the calculations. To satisfy stoichiometry and electrical neutrality, additional sodium ions would have to be disordered among interstices between water molecules or between anion oxygen atoms and water molecules. The contacts between anion atoms and water molecules, given in Table VII, and between water molecules, given in Table VIII, are

(31) K. Nakatsu, M. Shiro, *Y.* Saito, and **H** Ruroya, *Bull. Chem. SOC. Japan,* **SO,** 158 (1957).

long enough to permit interstitial sodium ions. If such a site were occupied with 20% probability, the electron density therein would be comparable to that of a lithium ion and thus would not be detectable with certainty in the presence of so many heavy atoms.

The high temperature factors of some of the water molecules are attributed to partial site occupation, consistent with the efflorescence of the compound. Allowing for a sixth water molecule coordinated to Na(5), there are 25 water molecules in the asymmetric unit, in agreement with the stoichiometry.

The success of the structure determination supports the correlation of structure and properties used in the solution of the structure. The octahedral coordination of manganese (IV) is to be expected on the basis of its d3 electron configuration, because of its high crystal field stabilization energy with respect to other geometries. It would be interesting to carry out a complete structure determination of the 9-molybdomanganate (IV) anion, $MnMo₉O₈₂⁶$, and then compare the geometries of the manganese(1V) in the niobate and molydate and correlate them with spectroscopic and magnetic data. (Only a two-dimensional heavy-atom determination of the $\text{MnMo}_{9}\text{O}_{32}$ ⁶⁻ structure was carried out by Waugh, *et al.*³²).

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> CONTRIBUTION FROM THE DEPARTMENT OF CHEMISTRY, THE UNIVERSITY OF ARIZOXA, TUCSON, ARIZONA 85721

Transition Metal Nitrosyls. VIII. Complexes of Chromium and Molybdenum

BY ROBERT D. FELTHAM, W. SILVERTHORN,¹⁰ AND G. MCPHERSON^{1b}

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Several new nitrosyl complexes of chromium and molybdenum have been synthesized including *trans*-[CrClNO(das)₂]ClO₄, cis,cis-MoCl₂(NO)₂(das), and cis,cis-MoCl₂(NO)₂(en). The chromium complex trans-CrClNO(das)₂⁺ has a doublet ground state and the esr spectrum shows hyperfine splitting due to both the nitrogen and arsenic nuclei. The measured values of the isotropic hyperfine parameters are $A_{\text{As}} = 35$ G and $A_N = 5$ G. The molybdenum compounds are diamagnetic and slowly isomerize to the mononitrosyl hyponitrito complexes $\{[MoCINO(das)]_2N_2O_2\}Cl_2$ and $\{[MoCINO(en)]_2N_2O_2\}Cl_2$. The firstorder rate constants for these isomerization reactions at 25° are 1.10×10^{-4} and 1.13×10^{-5} sec⁻¹, respectively.

Introduction

The past several papers in this series have described the preparation and characterization of mononitrosyl derivatives of iron and cobalt.^{2,3} These iron and cobalt

(1) **(a)** Taken in part from the Ph.D. Thesis of **W.** *S.,* University of

(2) W. Silverthoin and R. **I).** Feltham, *I?zovg. Chem., 6,* 1662 (1967).

(3) R. D. Feltham and R. **S.** Syholni, *ibid.,* **4,** 1334 (1965). **(4)** L. Dahl, private communication.

nitrosyl complexes, stabilized with o-phenylenebis-(dimethylarsine) (das) and ethylenediamine (en), have structures in which the metal, nitrogen, and oxygen atoms are not collinear.⁴ The best formalism for discussing these compounds is the valence bond structure Arizona, 1967; Shell Fellow, 1966-1967: **(b)** NSF Undergraduate Research in which an N=O- group is bound to the metal *via* the Participant, 1965. no metal atom. This description is explicit in demand-